Spatial Data Science

Metropolitan Data I

(YMS31303)

Lecture 3

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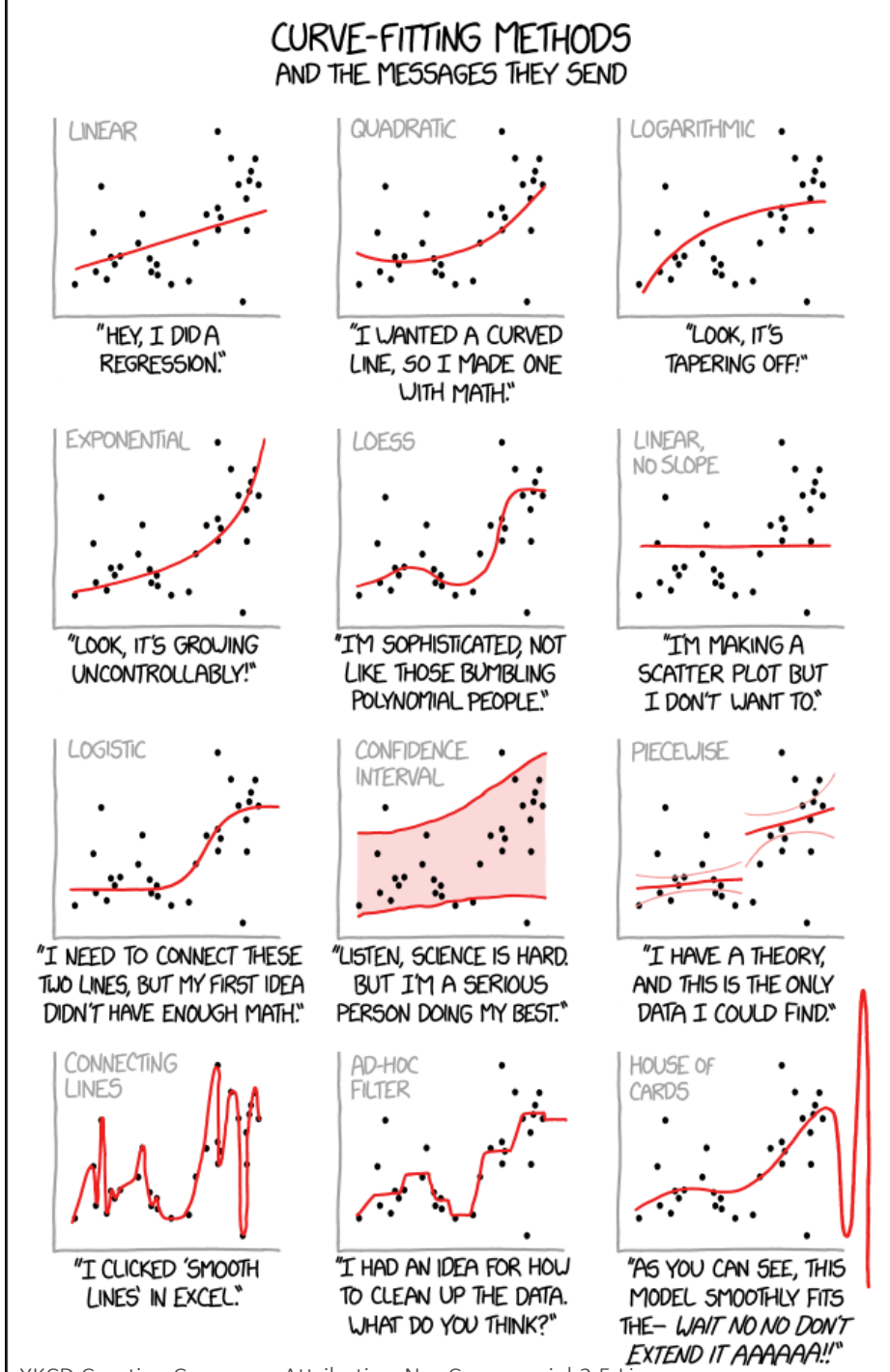
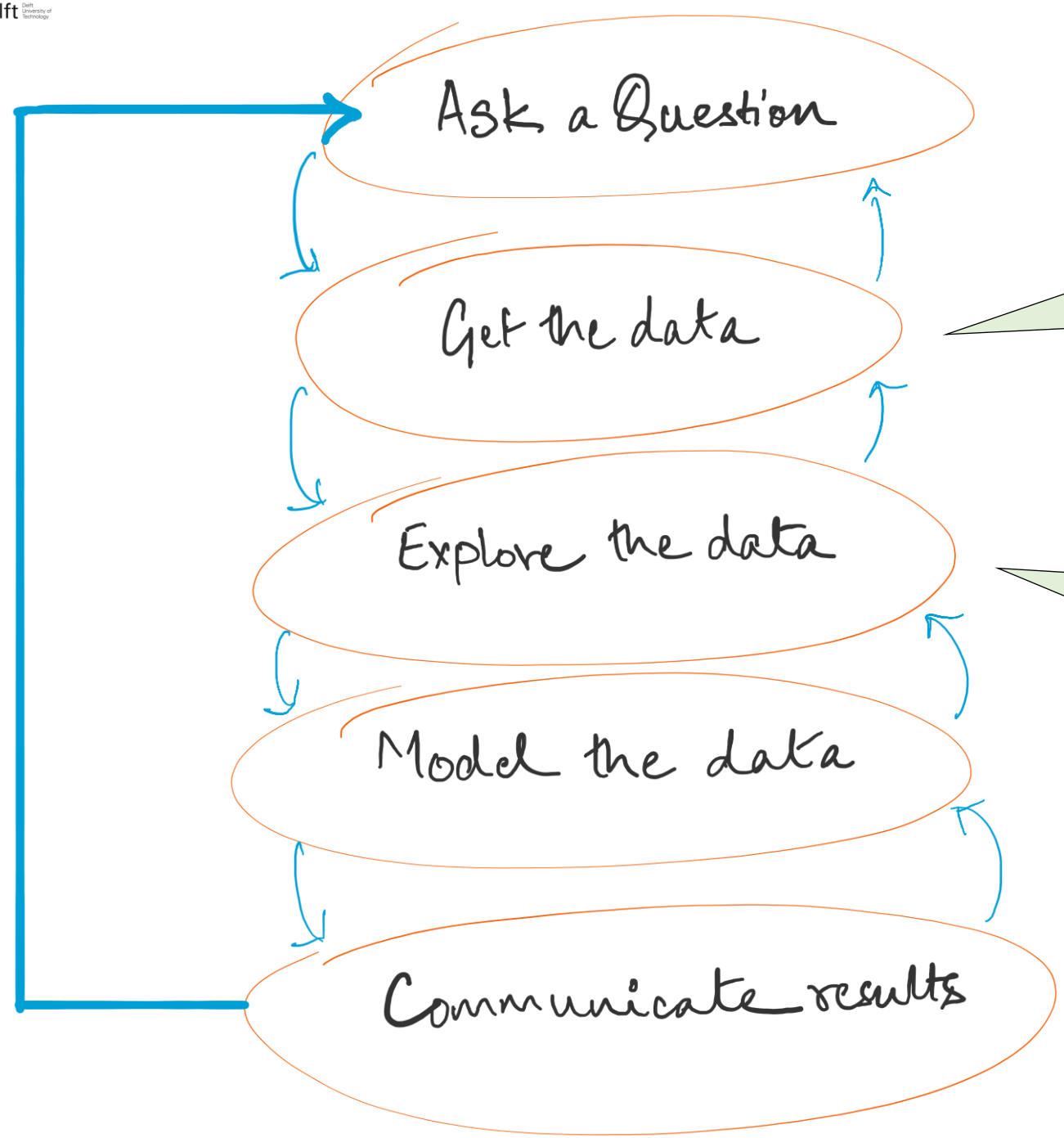


Last Time

- Types of Data
- Grammar
- EDA without Pandas
- EDA with Pandas
- Data Concerns

Today

- Descriptive Statistics
- Break
- Data Transformations



How were the data **sampled**?
Which data are **relevant**?
Are there **privacy** issues?

Plot the data.
Are there **anomalies**?
Are there **patterns**?

Descriptive Statistics

Basics of Sampling

Population versus sample:

- A **population** is the entire set of objects or events under study. Population can be hypothetical “all students” or all students in this class.
- A **sample** is a “representative” subset of the objects or events under study. Needed because it’s impossible or intractable to obtain or compute with population data.

Biases in samples:

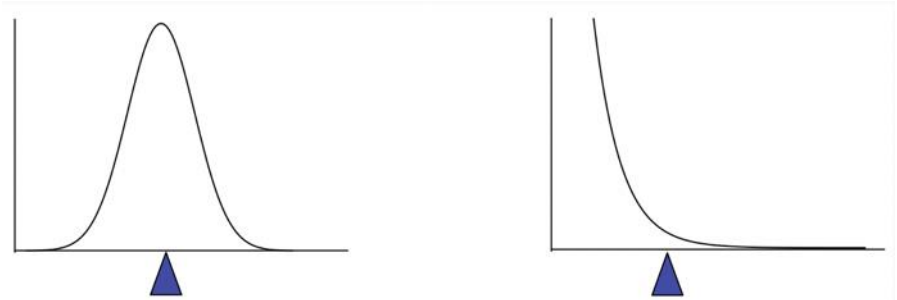
- **Selection bias**: some subjects or records are more likely to be selected
- Volunteer/**nonresponse bias**: subjects or records who are not easily available are not represented

Examples?

Sample mean

- The **mean** of a set of *n* observations of a variable is denoted $\bar{x}$ and is defined as:

$$\bar{x} = \frac{x_1 + x_2 + \cdots + x_n}{n} = \frac{1}{n}\sum_{i=1}^{n} x_i$$



- The mean describes what a “typical” sample value looks like, or where is the “center” of the distribution of the data.
- **Important** : there is always uncertainty involved when calculating a sample mean to estimate a population mean.

Sample median

- The **median** of a set of n number of observations in a sample, ordered by value, of a variable is defined by

$$\text{Median} = \begin{cases} x_{(n+1)/2} & \text{if } n \text{ is odd} \\ \frac{x_{n/2} + x_{(n+1)/2}}{2} & \text{if } n \text{ is even} \end{cases}$$

- Example (already in order):

  Ages: 17, 19, 21, 22, 23, 23, 23, 38

  Median = (22+23)/2 = 22.5

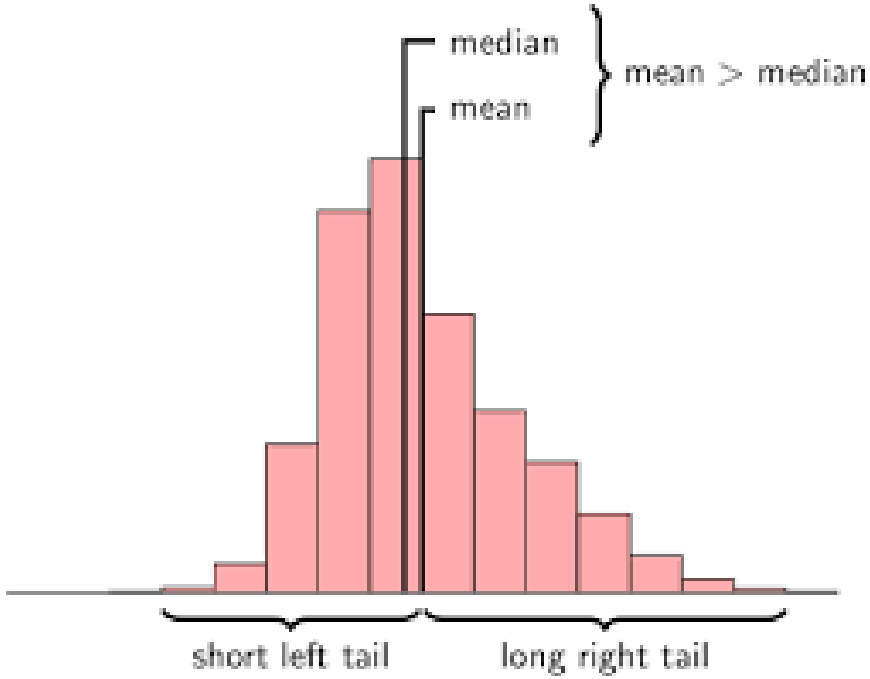
- The median also describes what a typical observation looks like, or where is the center of the distribution of the sample of observations.

Mean vs Median

The mean is sensitive to extreme values **(outliers)**

Mean, median, and skewness

The mean is sensitive to outliers:

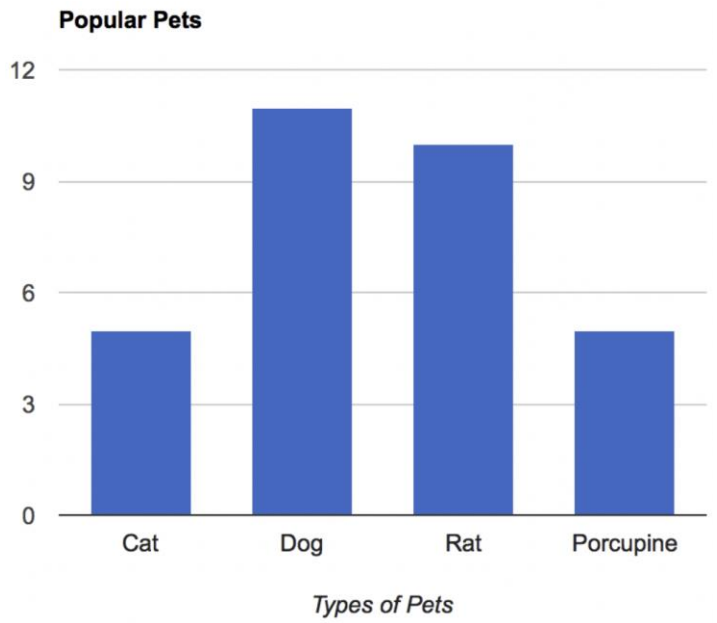


The above distribution is called **right-skewed** since the mean is greater than the median.

Note: **skewness** often “follows the longer tail”.

Regarding Categorical Variables…

For categorical variables, neither mean or median make sense. Why?



The mode might be a better way to find the most “representative” value.

Measures of Spread: Range

The spread of a sample of observations measures how well the mean or median describes the sample.

One way to measure spread of a sample of observations is via the **range**.

Range (R) = (Max)imum Value - (Min)imum Value

Measures of Spread: Variance

- The (sample) **variance**, denoted s^2, measures how much on average the sample values deviate from the mean:

$$s^2 = \frac{1}{n-1}\sum_{i=1}^{n} |x_i - \bar{x}|^2$$

- Note: the term $|x_i - \bar{x}|$ measures the amount by which each x_i deviates from the mean $\bar{x}$. Squaring these deviations means that s^2 is sensitive to extreme values (outliers).
- Note: s^2 doesn't have the same units as the x_i :(
- What does a variance of 1,008 mean? Or 0.0001?

Measures of Spread: Standard Deviation

The (sample) **standard deviation**, denoted *s (or sigma)*, is the square root of the variance

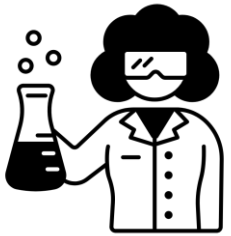
$$s = \sqrt{s^2} = \sqrt{\frac{1}{n-1}\sum_{i=1}^{n} |x_i - \bar{x}|^2}$$

Note: *s* does have the same units as the x_i. Phew!

Break

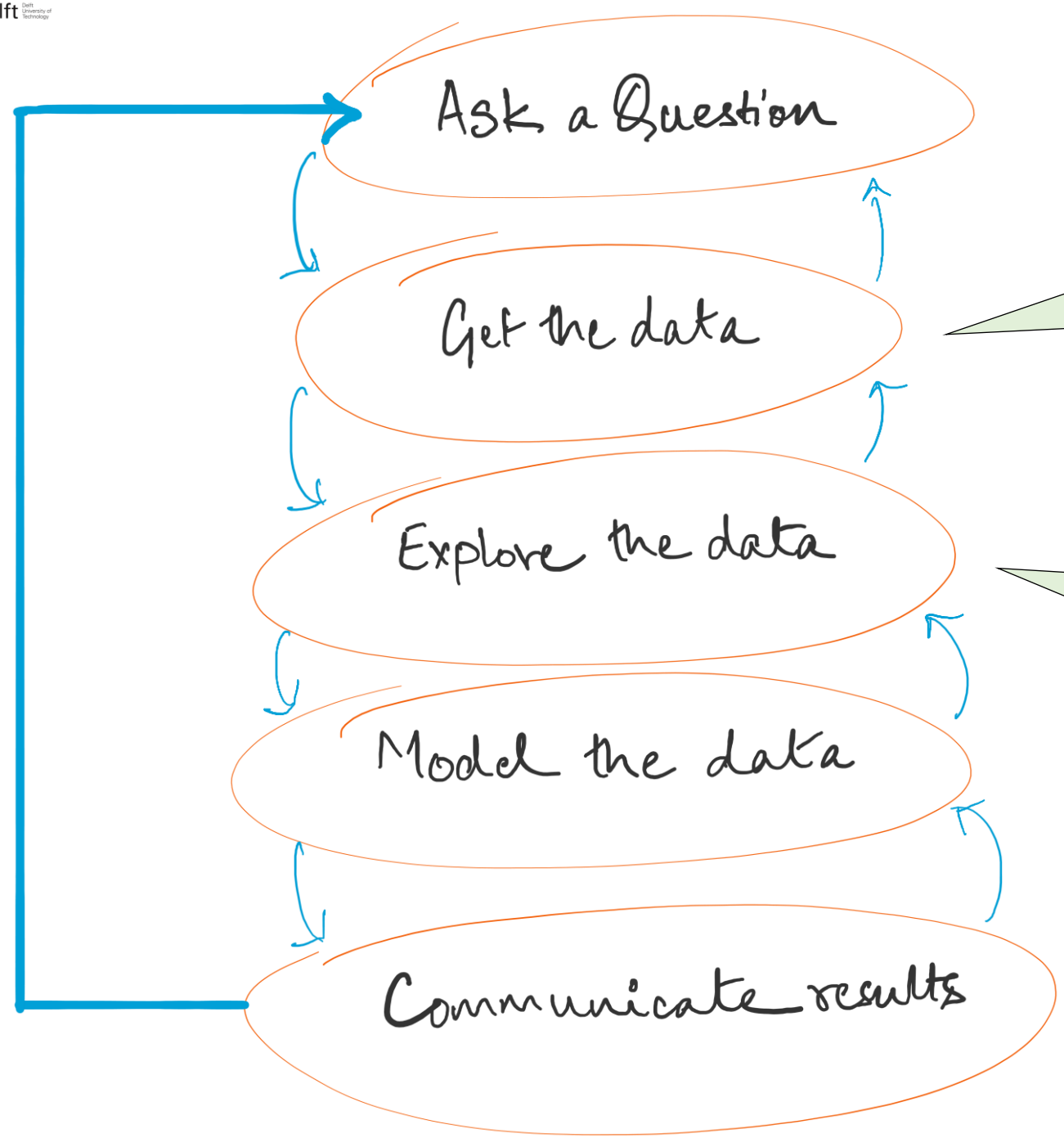
CHILL

WALK



COFFEE OR TEA

MAKE FRIENDS



How were the data **sampled**?
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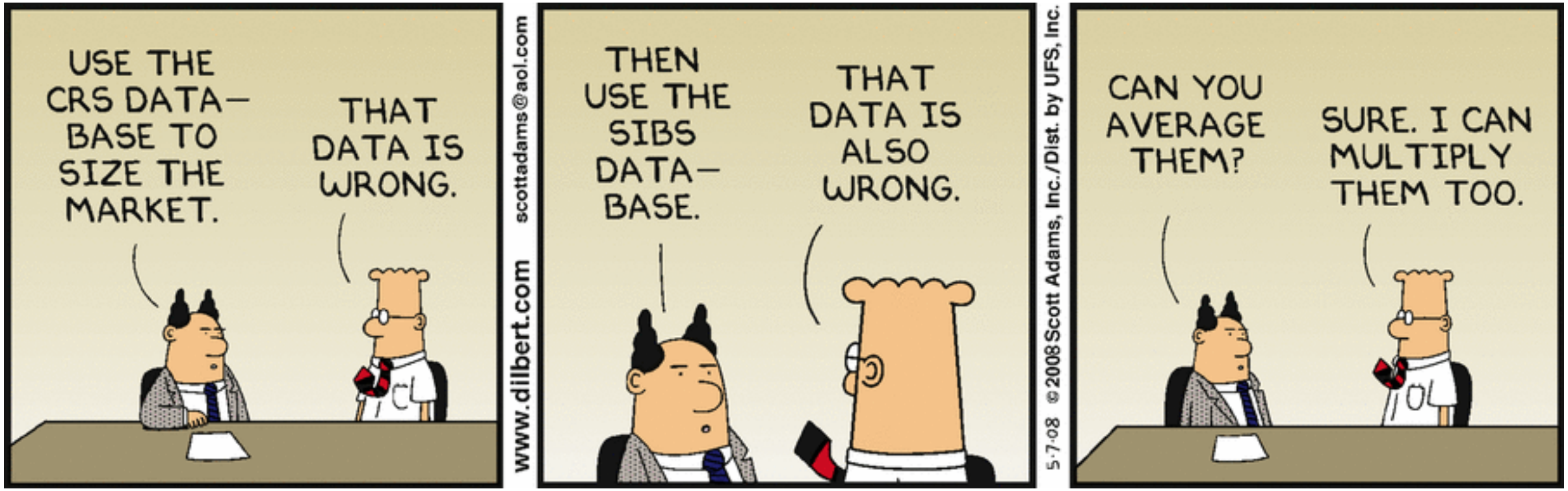
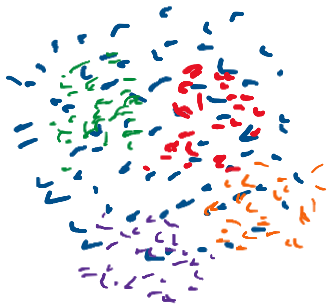
Data Science Process	**Inclusion** *Who is (not) included in the data?*	**Inequality** *What role does inequality play in data science methods?*	**Participation** *Who is (not) involved in the data science process?*	**Power** *How does the data reflect existing power dynamics?*	**Positionality** *What is your own positionality with the research?*
Transform Data *Completeness, Missing data, Consistency, Pluralism & Accuracy of collected data*	Do not only consider what data is missing from the dataset, but also whose data is missing (diversity in variables, but also diversity in sources).	Are you erasing or magnifying someone's perspective by cleaning the data (aggregating, replacing missing value, or slicing)? (Boyd, 2021a). Did the (joint) distribution of the data change after cleaning? If so, explore the impacts of a different cleaning approach.	Ensure transparency of data cleaning choices. Collaboratively discuss the impact of these decisions and alternative ways of transforming the data.	Are the data cleaning techniques (normalization, replacement of missing values) reinforcing a dominant framing of what the data should show? (Boyd, 2021a).	Critically reflect on your data cleaning choices? 1. Why are you using these specific data cleaning methods? 2. How are you silencing certain voices in your data cleaning process? And why? 3. How are you amplifying certain voices in your data cleaning process? And why?

Data Transformations

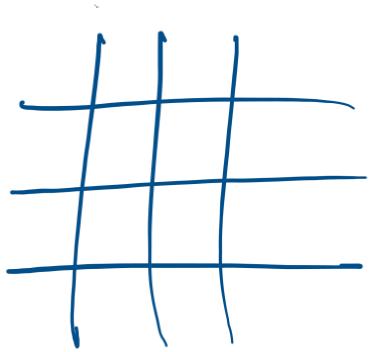
Why Transform Data



feature engineering



RAW



TABULAR

features

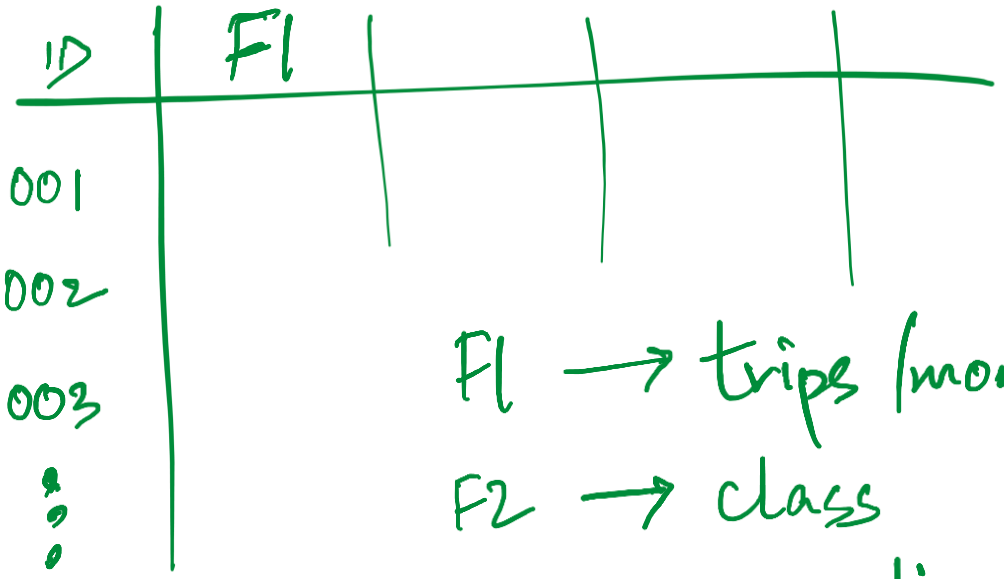
objects	f_1	f_2	...
O1			
O2			
⋮			

Based upon Domain knowledge

Eg. SMART-CARD CHECK-IN LOGS

Features (measurable)

* Users



F1 → trips/month

F2 → class

F3 → Avg. time of trip

F4 → total price

⋮

* Alternative: trips/station

Why Scaling

- Comparison of groups of Object

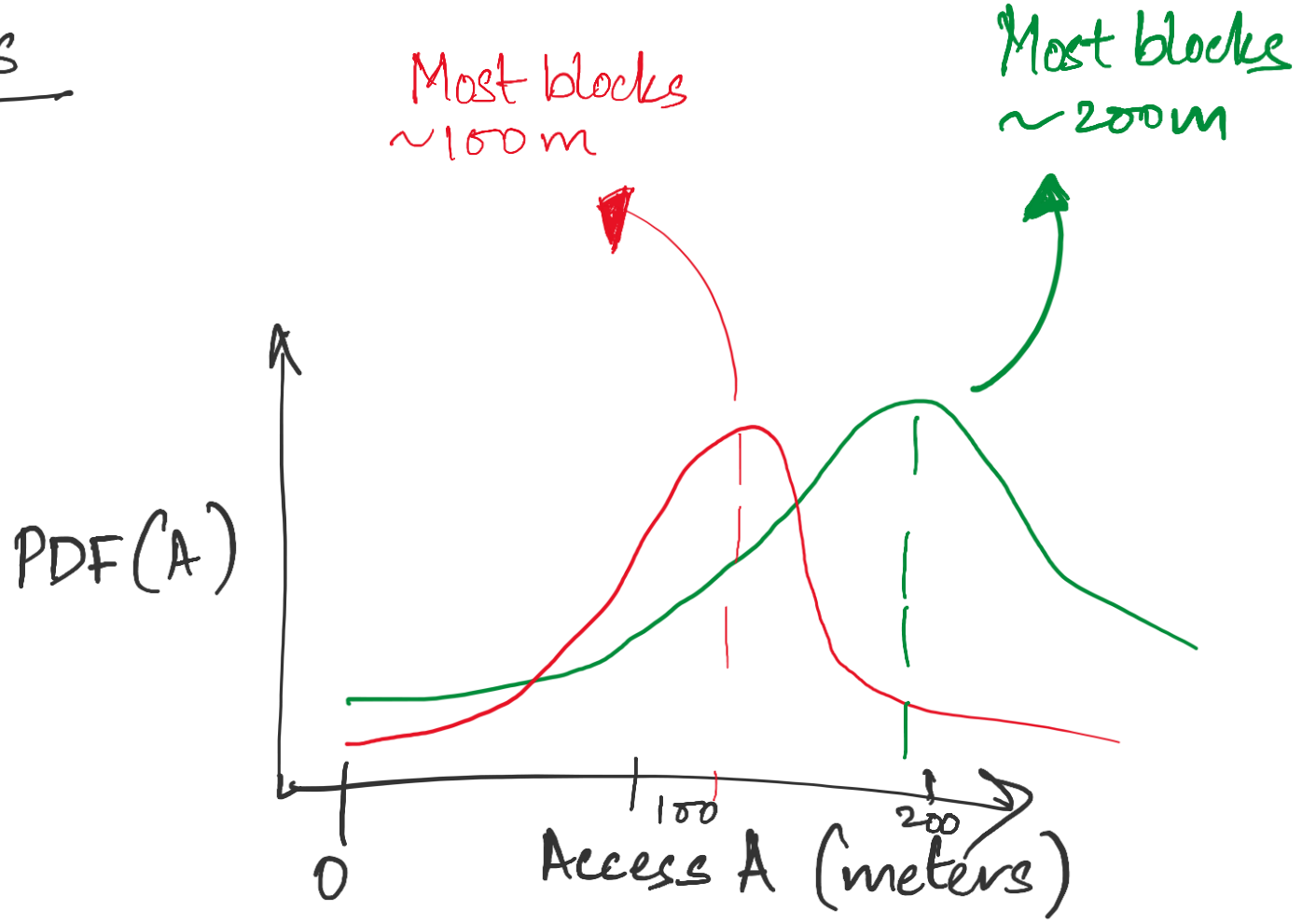
Example: Access to infrastructure in Cities

Photo by Joe Mann/AFP/Getty Images

Example of Access

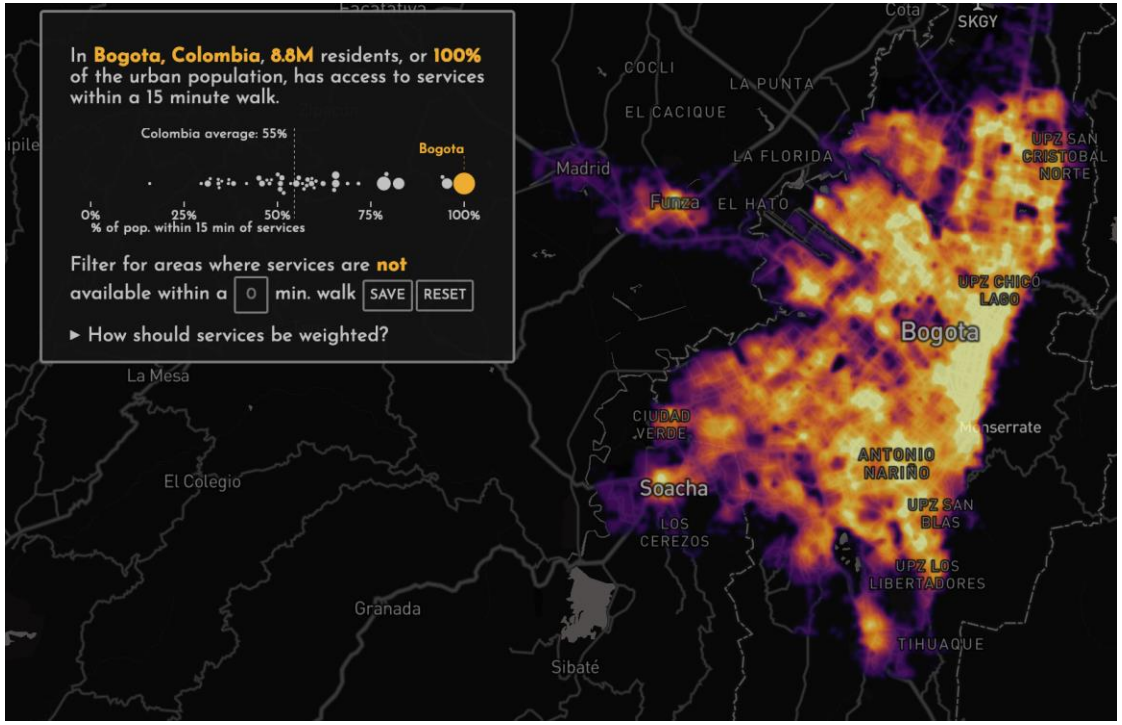
City 1	A1

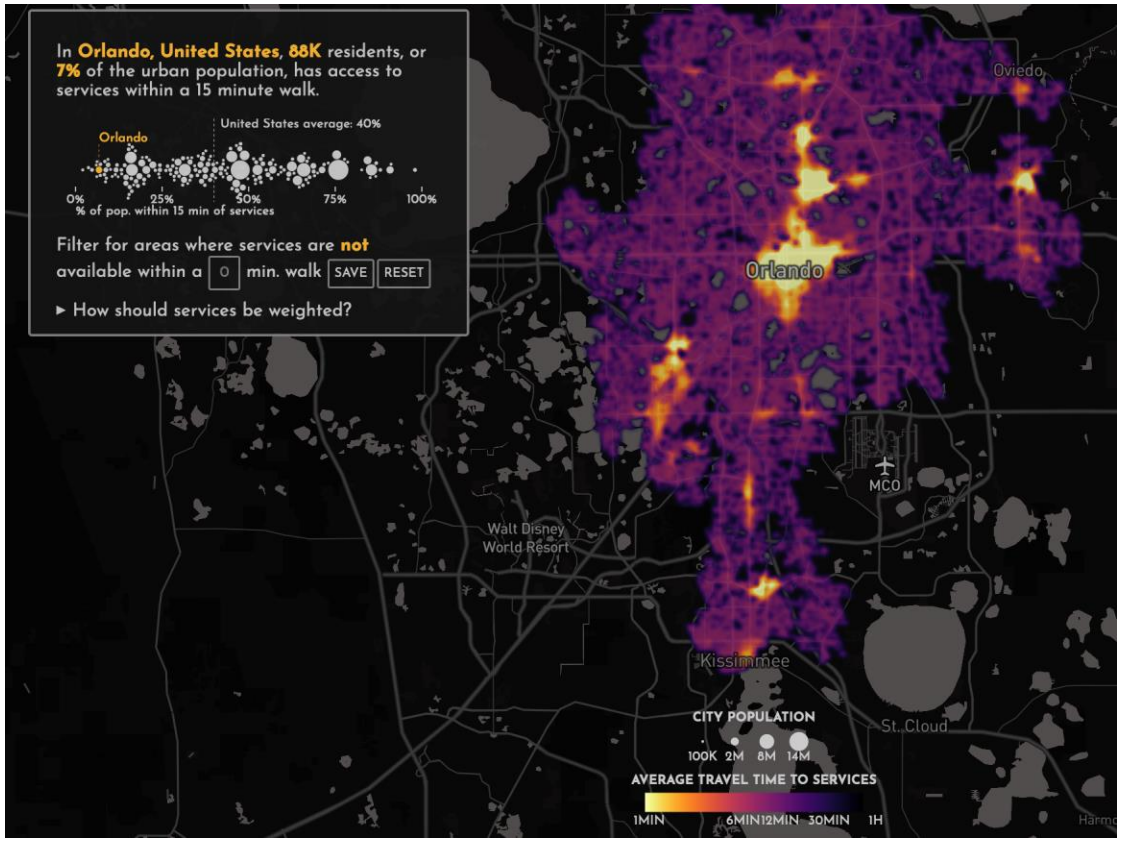
City 2	A2



Can we compare these cities?

Nicoletti, L., Sireno, M., & Verma, T. (2021). Unequal Access to Urban Infrastructure in Cities across the World. In Preparation.





Why Scaling

- Comparison of groups of Object

Example: Access to infrastructure in Cities

- ML algorithms use Euclidean distance (higher magnitude will weigh more) –

advanced topics will be explored in week 6-7

Photo by Joe Mann/AFP/Getty Images

Scale Data

F1 F2 F3 F4

Dimensions

1 – 500 trips/month

200 – 2000 CHF/month

Photo by Joe Mann/AFP/Getty Images

Normalisation

- Transformation of data to a different range [a - b]
- Normally [0-1]
- Create new variables from the transformations.

$$X_i' = \frac{X_i - \min(x)}{\max(x) - \min(x)} \times [b - a] + a$$

Rescaled value

Original value

Min value in feature

New range

Photo by Joe Mann/AFP/Getty Images

Standardisation

or, Z-score normalisation

- Transformation of data to a different range that is normally distributed with mean 0 and standard deviation 1.

$$N(\mu=0, \sigma=1)$$

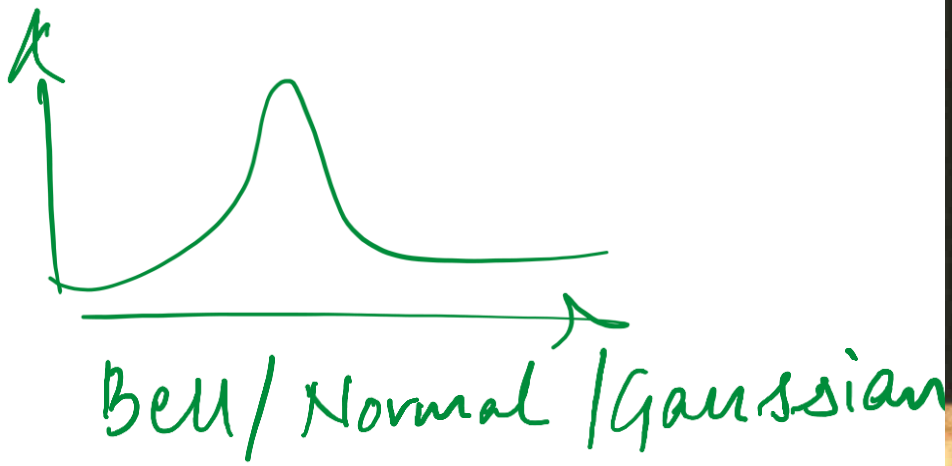
Rescaled value

$$X_i' = \frac{X_i - \mu_i}{\sigma_i}$$

Photo by Joe Mann/AFP/Getty Images

Use S (All others N)

- Features are normally distributed (**not normalisation**)



- Many outliers (normalisation squashes them in a limited range)
- All unsupervised learning algorithms, like clustering or dimensionality reduction

Photo by Joe Mann/AFP/Getty Images

Dealing with Missing Data

- If your data is big, sacrifice examples with missing features
- Data Imputation techniques
  - Use average of the feature for replacing a missing value $x_1^0 \leftarrow \bar{x}$
  - **Advanced**: regression modelling to estimate missing values

For next class..

Finish Labs to practice programming

Complete Homework for more practice

Check Assignment contents and due date

See “To do before class” for next lecture (~ 1 hour of self-study)